

# General Certificate of Education

# Mathematics 6360

MFP2 Further Pure 2

# Mark Scheme

# 2006 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

## **Key To Mark Scheme And Abbreviations Used In Marking**

M	mark is for method				
m or dM	mark is dependent on one or more M marks and is for method				
A	mark is dependent on M or m marks and is for accuracy				
В	mark is independent of M or m marks and is for method and accuracy				
Е	mark is for explanation				
$\sqrt{\text{or ft or F}}$	follow through from previous				
	incorrect result	MC	mis-copy		
CAO	correct answer only	MR	mis-read		
CSO	correct solution only	RA	required accuracy		
AWFW	anything which falls within	FW	further work		
AWRT	anything which rounds to	ISW	ignore subsequent work		
ACF	any correct form	FIW	from incorrect work		
AG	answer given	BOD	given benefit of doubt		
SC	special case	WR	work replaced by candidate		
OE	or equivalent	FB	formulae book		
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme		
–x EE	deduct x marks for each error	G	graph		
NMS	no method shown	c	candidate		
PI	possibly implied	sf	significant figure(s)		
SCA	substantially correct approach	dp	decimal place(s)		

#### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

# MFP2

Total  Total  7  2(a) $\dot{x} = 1 - t^2, \dot{y} = 2t$ $\dot{x}^2 + \dot{y}^2 = \left(1 - t^2\right)^2 + 4t^2$ $= \left(1 + t^2\right)^2$ A1  A3  AG; must be intermediate line  (b) $S = 2\pi \int_{1}^{2} \left(1 + t^2\right) t^2 dt$ $= 2\pi \left[\frac{t^3}{3} + \frac{t^5}{5}\right]_{1}^{2}$ $= 2\pi \left[\frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ A1	Q	Solution	Marks	Total	Comments
$A = 1, B = -1$ $A1$ $A1F$ $A1F$ $Or$ $\frac{r^2 + r - 1}{r^2 + r} = 1 - \frac{1}{r(r+1)}$ $B1$ $= 1 - \left(\frac{1}{r} - \frac{1}{r+1}\right)$ $M1A1$ $Do not allow M1 if merely$ $\sum \frac{1}{r} - \sum \frac{1}{r+1} \text{ is summed}$ $A1 for suitable (3 at least) number of row$ $Sum = 98 + \frac{1}{100}$ $= 98.01$ $M1$ $= 98.01$ $M1$ $= 98.01$ $M1$ $= 98.01$ $M1$ $= (1 + t^2)^2 + 4t^2$ $= (1 + t^2)^2 + 4t^2$ $= (1 + t^2)^2$ $A1$ $M1$ $= (2a)$ $x = 1 - t^2, y = 2t$ $x^2 + y^2 = (1 - t^2)^2 + 4t^2$ $= (1 + t^2)^2$ $A1$ $M1$ $= (1 + t^2)^2$ $A1$ $M1$ $= 2\pi \left[\frac{t^3}{3} + \frac{t^5}{5}\right]_1^1$ $= 2\pi \left[\frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{15} - \frac{1}{5} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{8}{15} + \frac{32}{15} - \frac{1}{5} - \frac{1}{5}\right]$ $= 2\pi \left[\frac{1}{15} + \frac{1}{15} + \frac{1}{15} - \frac{1}{15} - \frac{1}{15} + \frac{1}{15} - $	1(a)	$r^2 + r - 1 = A(r^2 + r) + B$	M1		Any correct method
(b) $r = 1  1 - \frac{1}{1} + \frac{1}{2}$ $r = 2  1 - \frac{1}{2} + \frac{1}{3}$ $r = 99  1 - \frac{1}{99} + \frac{1}{100}$ Sum $= 98 + \frac{1}{100}$ $= 98.01$ M1  2(a) $x = 1 - t^2 \cdot y = 2t$ $x^2 + y^2 = (1 - t^2)^2 + 4t^2$ $= (1 + t^2)^2$ A1  M1 $x = 2 + t^2 \cdot y = 4t^2$ $x = 1 - t^2 \cdot y = 2t$ $x = 1 - t^2 \cdot y = 2t$ A1  M1  M1  M1  Must have 98 or 99  OE Allow correct answer with no working 4 marks  (b) $x = 2\pi \int_{1}^{2} (1 + t^2) t^2 dt$ $x = 1 - t^2 \cdot y = 2t$ M1  Must be correct substitutions for M1  A1 Allow if one term integrated correctly  A1 Allow if one term integrated correctly  A2 Any form $x = 2 - t \int_{1}^{2} (1 + t^2) t^2 dt$ A1 Allow if one term integrated correctly  A2 Any form		A = 1, B = -1	A1		
(b) $r = 1  1 - \frac{1}{1} + \frac{1}{2}$ $r = 2  1 - \frac{1}{2} + \frac{1}{3}$ $r = 99  1 - \frac{1}{99} + \frac{1}{100}$ Sum = $98 + \frac{1}{100}$ = $98.01$ Must have $98 \text{ or } 99$ OE Allow correct answer with no working $\frac{1}{2} + \frac{1}{2} + \frac{1}{$			A1F	3	
(b) $r = 1  1 - \frac{1}{1} + \frac{1}{2}$ $r = 2  1 - \frac{1}{2} + \frac{1}{2}$ $r = 99  1 - \frac{1}{99} + \frac{1}{100}$ Sum = $98 + \frac{1}{100}$ = $98.01$ Must have $98 \text{ or } 99$ OE Allow correct answer with no working $4 \text{ marks}$ Total  7  2(a) $\dot{x} = 1 - t^2, \dot{y} = 2t$ $\dot{x}^2 + \dot{y}^2 = (1 - t^2)^2 + 4t^2$ $= (1 + t^2)^2$ A1 3 AG; must be intermediate line  (b) $S = 2\pi \int_{1}^{2} (1 + t^2) t^2 dt$ $= 2\pi \left[ \frac{t^3}{3} + \frac{t^5}{5} \right]_{1}^{2}$ $= 2\pi \left[ \frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5} \right]$ $= 2\pi \left[ \frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5} \right]$ A1F Any form  A1F 5					` ,
$r = 2  1 - \frac{1}{2} + \frac{1}{3}$ $r = 99  1 - \frac{1}{99} + \frac{1}{100}$ $Sum = 98 + \frac{1}{100}$ $= 98.01$ $m1$ $A1F$					$=1-\left(\frac{1}{r}-\frac{1}{r+1}\right) M1A1$
$r = 2  1 - \frac{1}{2} + \frac{1}{3}$ $r = 99  1 - \frac{1}{99} + \frac{1}{100}$ $Sum = 98 + \frac{1}{100}$ $= 98.01$ $m1$ $A1F$	(b)	$r = 1$ $1 - \frac{1}{1} + \frac{1}{2}$			
$r = 99  1 - \frac{1}{99} + \frac{1}{100}$ $Sum = 98 + \frac{1}{100}$ $= 98.01$ $m1$ $A1F$ $4$ $Must have 98 or 99$ $OE Allow correct answer with no working 4 marks$ $x^2 + y^2 = (1 - t^2)^2 + 4t^2$ $= (1 + t^2)^2$ $A1$ $S = 2\pi \int_{1}^{2} (1 + t^2) t^2 dt$ $= 2\pi \left[ \frac{t^3}{3} + \frac{t^5}{5} \right]_{1}^{2}$ $= 2\pi \left[ \frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5} \right]$ $= 2\pi \left[ \frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5} \right]$ $= 2\pi \left[ \frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5} \right]$ $= 2\pi \left[ \frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5} \right]$ $= \frac{256\pi}{15}$ $A1F$ $A1$		2 1/ 1/	M1		Do not allow M1 if merely
$r = 99  1 - \frac{17}{99} + \frac{1}{100}$ $Sum = 98 + \frac{1}{100}$ $= 98.01$ $Sum = 98 + \frac{1}{100}$ $= 100$ $= 1$		$r = 2$ $1 - \frac{1}{2} + \frac{1}{3}$	1411		•
Sum = $98 + \frac{1}{100}$ $= 98.01$ m1 A1F A1F A1F A1F A1F A1F A1F A1F A1F A1		r = 00  1  1 /  1	A 1 E		, , , , ,
		7 - 99  1 - 99  + 100	AII		At for suitable (3 at least) number of rows
		$Sum = 98 + \frac{1}{100}$	m1		Must have 98 or 99
Total  Total  7  2(a) $\dot{x} = 1 - t^2, \dot{y} = 2t$ $\dot{x}^2 + \dot{y}^2 = \left(1 - t^2\right)^2 + 4t^2$ $= \left(1 + t^2\right)^2$ A1  A3  AG; must be intermediate line  (b) $S = 2\pi \int_{1}^{2} \left(1 + t^2\right) t^2 dt$ $= 2\pi \left[\frac{t^3}{3} + \frac{t^5}{5}\right]_{1}^{2}$ $= 2\pi \left[\frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ A1				4	OE Allow correct answer with no working
2(a) $\dot{x} = 1 - t^2, \dot{y} = 2t$ $\dot{x}^2 + \dot{y}^2 = \left(1 - t^2\right)^2 + 4t^2$ $= \left(1 + t^2\right)^2$ Al 3 AG; must be intermediate line  (b) $S = 2\pi \int_{1}^{2} \left(1 + t^2\right) t^2 dt$ $= 2\pi \left[\frac{t^3}{3} + \frac{t^5}{5}\right]_{1}^{2}$ $= 2\pi \left[\frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ Alf Allow if one term integrated correctly $= 2\frac{8}{15} = \frac{256\pi}{15}$ Alf Any form					
$\dot{x}^2 + \dot{y}^2 = \left(1 - t^2\right)^2 + 4t^2$ $= \left(1 + t^2\right)^2$ M1 A1 AG; must be intermediate line $S = 2\pi \int_{1}^{2} \left(1 + t^2\right) t^2 dt$ $= 2\pi \left[\frac{t^3}{3} + \frac{t^5}{5}\right]_{1}^{2}$ M1A1 Must be correct substitutions for M1 $= 2\pi \left[\frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ Allow if one term integrated correctly $= 2\pi \left[\frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5}\right]$ Any form $= \frac{256\pi}{15}$ A1F A1F 5	2(a)		D1	7	
(b) $S = 2\pi \int_{1}^{2} (1+t^{2}) t^{2} dt$ $= 2\pi \left[ \frac{t^{3}}{3} + \frac{t^{5}}{5} \right]_{1}^{2}$ $= 2\pi \left[ \frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5} \right]$ $= \frac{256\pi}{15}$ Must be correct substitutions for M1  Allow if one term integrated correctly  Any form	2(a)	v $v$ $v$ $v$ $v$	BI		
(b) $S = 2\pi \int_{1}^{2} (1+t^{2}) t^{2} dt$ $= 2\pi \left[ \frac{t^{3}}{3} + \frac{t^{5}}{5} \right]_{1}^{2}$ $= 2\pi \left[ \frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5} \right]$ $= \frac{256\pi}{15}$ Must be correct substitutions for M1  Allow if one term integrated correctly  Any form		$\dot{x}^2 + \dot{y}^2 = \left(1 - t^2\right)^2 + 4t^2$	M1		
$S = 2\pi \int_{1}^{\infty} (1+t^2) t^2 dt$ $= 2\pi \left[ \frac{t^3}{3} + \frac{t^5}{5} \right]_{1}^{2}$ $= 2\pi \left[ \frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5} \right]$ $= \frac{256\pi}{15}$ Must be correct substitutions for M1  Allow if one term integrated correctly  A1F  Any form		$=\left(1+t^2\right)^2$	A1	3	AG; must be intermediate line
$= 2\pi \left[ \frac{8}{3} + \frac{32}{5} - \frac{1}{3} - \frac{1}{5} \right]$ $= \frac{256\pi}{15}$ A1F Any form $5$	(b)	$S = 2\pi \int_{1}^{2} \left(1 + t^{2}\right) t^{2} dt$	M1A1		Must be correct substitutions for M1
$=\frac{256\pi}{15}$ A1F 5		$=2\pi \left[\frac{t^3}{3} + \frac{t^5}{5}\right]_1^2$	m1		Allow if one term integrated correctly
			A1F		Any form
		$=\frac{256\pi}{15}$	A1F	5	
1 0 1		Total		8	

Q	Solution	Marks	Total	Comments
3(a)(i)	$\frac{e^k + e^{-k}}{2} - \frac{3(e^k - e^{-k})}{2} = -1$	M1		Allow if 2's are missing or if coshx and sinhx interchanged
	$-2e^{k} + 4e^{-k} = -2$	A1		Sinix interchanged
	$-2e^{k} + 4e^{-k} = -2$ $e^{2k} - e^{k} - 2 = 0$ $(e^{k} + 1)(e^{k} - 2) = 0$ $e^{k} \neq -1$ $e^{k} = 2$	A1	3	AG Condone <i>x</i> instead of <i>k</i>
(ii)	$\left(e^k + 1\right)\left(e^k - 2\right) = 0$	M1		
	$e^k \neq -1$	E1		Must state something to earn E1. Do not
	$e^k = 2$	A1		accept ignoring or crossing out.
	$k = \ln 2$	A1F	4	
(b)(i)	$ \cosh x = 3\sinh x $ or in terms of $e^x$	M1		
	$\tanh x = \frac{1}{3} \text{ or } 2e^x = 4e^{-x}$	<b>A</b> 1		
	$x = \frac{1}{2} \ln \left( \frac{1 + \frac{1}{3}}{1 - \frac{1}{3}} \right)$ or $e^{2x} = 2$	A1F		
	$x = \frac{1}{2} \ln 2$	A1	4	CAO
(ii)	$\frac{\mathrm{d}y}{\mathrm{d}x} = \sinh x - 3\cosh x  \text{or}  -\mathrm{e}^x - 2\mathrm{e}^{-x}$	M1		
	$= 0$ when $\tanh x = 3$ or $e^{2x} = -2$	A1		
	Correct reason	E1	3	Must give a reason
(iii)	$\frac{d^2 y}{dx^2} = y = 0$ at $(\frac{1}{2} \ln 2, 0)$	B1F	1	
	ie one point			
	Total		15	

MFP2 (cont) Q	Solution	Marks	Total	Comments
4	× ×			
(a)(i)	Circle	B1		
	Correct centre	B1		
	Enclosing the origin	B1	3	
(ii)	Half line	B1		
	Correct starting point	B1		
	Correct angle	B1	3	
(b)	Correct part of the line <b>indicated</b>	B1F	1	
(~)	Total	211	7	
5(a)(i)	$\alpha + \beta + \gamma = 4i$	B1	1	
(ii)	$\alpha\beta\gamma = 4-2i$	B1	1	
(b)(i)	$\alpha + \alpha = 4i$ , $\alpha = 2i$	B1	1	AG
(ii)	$\beta \gamma = \frac{4-2i}{2i} = -2i -1$	M1		Some method must be shown, eg $\frac{2}{i}$ – 1
	21	A1	2	AG
(iii)	$q = \alpha \beta + \beta \gamma + \gamma \alpha$	M1		
	$=\alpha(\beta+\gamma)+\beta\gamma$	M1		Or $\alpha^2 + \beta \gamma$ , ie suitable grouping
	$= 2i \cdot 2i - 2i - 1 = -2i - 5$	A1	3	AG
		3.61		
(c)	Use of $\beta + \gamma = 2i$ and $\beta \gamma = -2i - 1$	M1		Elimination of say $\gamma$ to arrive at
	$z^2 - 2iz - (1 + 2i) = 0$	A1	2	$\beta^2 - 2i\beta - (1+2i) = 0$ M1A0 unless
				also some reference to $\gamma$ being a root AG
(d)	f(-1) = 1 + 2i - 1 - 2i = 0	M1		For any correct method
	$\beta = -1$ , $\gamma = 1 + 2i$	A1A1	3	A1 for each answer
	Total		13	

Q	Solution	Marks	Total	Comments
6(a)	$f(n+1)-8f(n)=15^{n+1}-8^{n-1}$			
	$-8(15^n - 8^{n-2})$	M1A1		
	$=15^{n+1}-8.15^n$			
	$=15^n (15-8)$	M1		For multiples of powers of 15 only
	$=7.15^{n}$	A1	4	For valid method ie not using 120 <sup>n</sup> etc
(b)	Assume $f(n)$ is $M(7)$			
	Then $f(n+1) - 8f(n) = 7 \times 15^n$	M1		Or considering $f(n+1)-f(n)$
	f(n+1) = M(7) + M(7)			
	= M(7)	A1		
	$n = 2$ : $f(n) = 15^2 - 8^0 = 224$			
	$= 7 \times 32$	B1		n=1 B0
	$P(n) \Rightarrow P(n+1)$ and $P(2)$ true	E1	4	Must score previous 3 marks to be awarded E1
	Total		8	

Q Q	Solution	Marks	Total	Comments
7(a)	2 <i>k</i> πi	M1		
	$z = e^{-\frac{\pi}{6}}$ , $k = 0, \pm 1, \pm 2, 3$	A2,1,0	3	OE
				M1A1 only if:
				(1) range for $k$ is incorrect eg 0,1,2,3,4,5
(b)(i)	2			(2) i is missing
(0)(1)	$\frac{w^2 - 1}{w} = w - \frac{1}{w} = 2i\sin\theta$	M1A1	2	AG
	w $w$			
(ii)	$\frac{w}{w} = \frac{1}{w}$	3.61		
	$\frac{w}{w^2 - 1} = \frac{1}{2i\sin\theta}$	M1		
		A1	2	AG
	$=-\frac{\mathrm{i}}{2\sin\theta}$	***	_	
(iii)	$2i  -2iw^{-1}i$	3.54		On for 1
	$\frac{2i}{w^2 - 1} = \frac{-2iw^{-1}i}{2\sin\theta}$	M1		Or for $\frac{1}{\sin \theta} e^{i\theta}$
	$=\frac{1}{\sin\theta}(\cos\theta-\mathrm{i}\sin\theta)$	A1		
	$= \cot \theta - i$	A1	2	
	$= \cot \theta - 1$	AI	3	AG
(IV)	$z = \frac{2i}{w^2 - 1} \text{ Or } z + 2i = \frac{2i}{w^2 - 1} + 2i$	M1		ie any correct method
	$w^2 - 1$ $w^2 - 1$			
	$z + 2i = zw^2$	A1	2	AG
(c)(i)	No coefficient of $z^6$	E1	1	
	$(w^2)^6 = 1$ $w^2 = e^{\frac{k\pi i}{3}}$ $z = \cot \frac{k\pi}{6} - i$ , $k = \pm 1, \pm 2, 3$	B1		Alternatively:
	kπ	3.61		$z + 2i = e^{\frac{k\pi i}{3}}z \qquad B1$ $z = \frac{2i}{\frac{k\pi i}{2}} \qquad M1$
	$z = \cot \frac{\pi}{6} - i$ , $k = \pm 1, \pm 2, 3$	M1 A2,1,0	1	$z+21=e^{-3}z$ B1
	· ·	A2,1,0	+	$z = \frac{2i}{1 + i}$ M1
				$\frac{k\pi i}{e^{3}-1}$
				roots A2,1,0
				(NB roots are $\pm \sqrt{3} - i$ ; $\pm \frac{1}{\sqrt{3}} - i$ ; $-i$ )
	Total		17	
	TOTAL		75	